

Parametric NAFEMS LE10 benchmark with tet elements

Comparison of resource consumption for different FEA programs

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1 Architecture

| | |
|--------|--|
| Date | Thu Sep 28 14:03:11 UTC 2023 |
| Host | Linux ip-172-31-44-208 6.2.0-1012-aws #12~22.04.1-Ubuntu SMP Thu Sep 7 14:01:24 UTC 2023 x86_64 x86_64 x86_64 GNU/Linux |
| CPU | Intel(R) Xeon(R) Platinum 8259CL CPU @ 2.50GHz |
| Number | 2 |
| Memory | 16066232 kB |

Figure 1: Architecture from `lstopo`

2 Codes & versions

2.1 aster

```
<INFO> Version exploitation 14.6.0 - 11/06/2020 - rev. b3490fa3b76c
```

2.2 calculix

```
This is Version 2.21
```

2.3 feenox

```
FeenoX v0.3.220-geb7bd44
a cloud-first free no-fee no-X uniX-like finite-element(ish) computational engineering tool

Last commit date    : Thu Sep 28 08:11:45 2023 -0300
Build date         : Thu Sep 28 13:47:20 2023 +0000
Build architecture : linux-gnu x86_64
Compiler version   : gcc (Ubuntu 11.4.0-lubuntu1~22.04) 11.4.0
Compiler expansion : gcc -Wl,-Bsymbolic-functions -fno-fat-lto-objects -fno-fat-lto -Wl,-z,relro -I /usr/include/x86_64-linux-gnu/mpich -L/usr/lib/x86_64-linux-gnu -lmpich
Compiler flags     : -O3 -fno-fat-lto -no-pie
Builder           : ubuntu@ip-172-31-44-208
GSL version       : 2.7.1
SUNDIALS version  : N/A
PETSc version     : Petsc Release Version 3.19.5, Aug 30, 2023
PETSc arch        : double-int32-release
PETSc options     : --download-eigen --download-hdf5 --download-hypre --download-metis --download-mumps --download-parmetis --download-scalapack --download-slepc --with-64-bit-indices=no --with-debugging=no --with-precision=double --with-scalar-type=real COPTFLAGS=-O3 CXXOPTFLAGS=-O3 FOPTFLAGS=-O3
SLEPC version     : SLEPC Release Version 3.19.1, unknown
```

2.4 reflex

```
Reflex Version: v1.12.3-1024-ga9e74e0ed
```

2.5 sparselizard

```
v.2022.05-53-g37a9d2b1
```

3 Reference solution

```
$ time feenox le10-ref.fee
sigma_y(D) = -5.3773 MPa (616323 degrees of freedom)
127.19user 3.46system 2:10.86elapsed 99%CPU (0avgtext+0avgdata 3485056maxresident)k
0inputs+0outputs (0major+1815753minor)pagefaults 0swaps
$
```

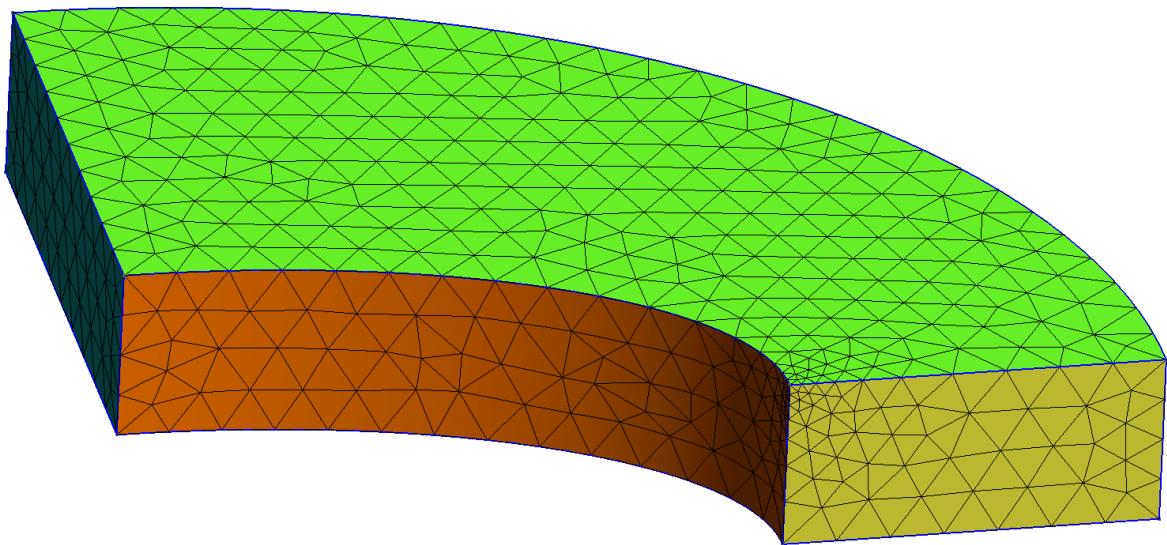


Figure 2: Coarser tet mesh for $c = 1$

4 Figures

Parametric NAFEMS LE10 benchmark with tet elements

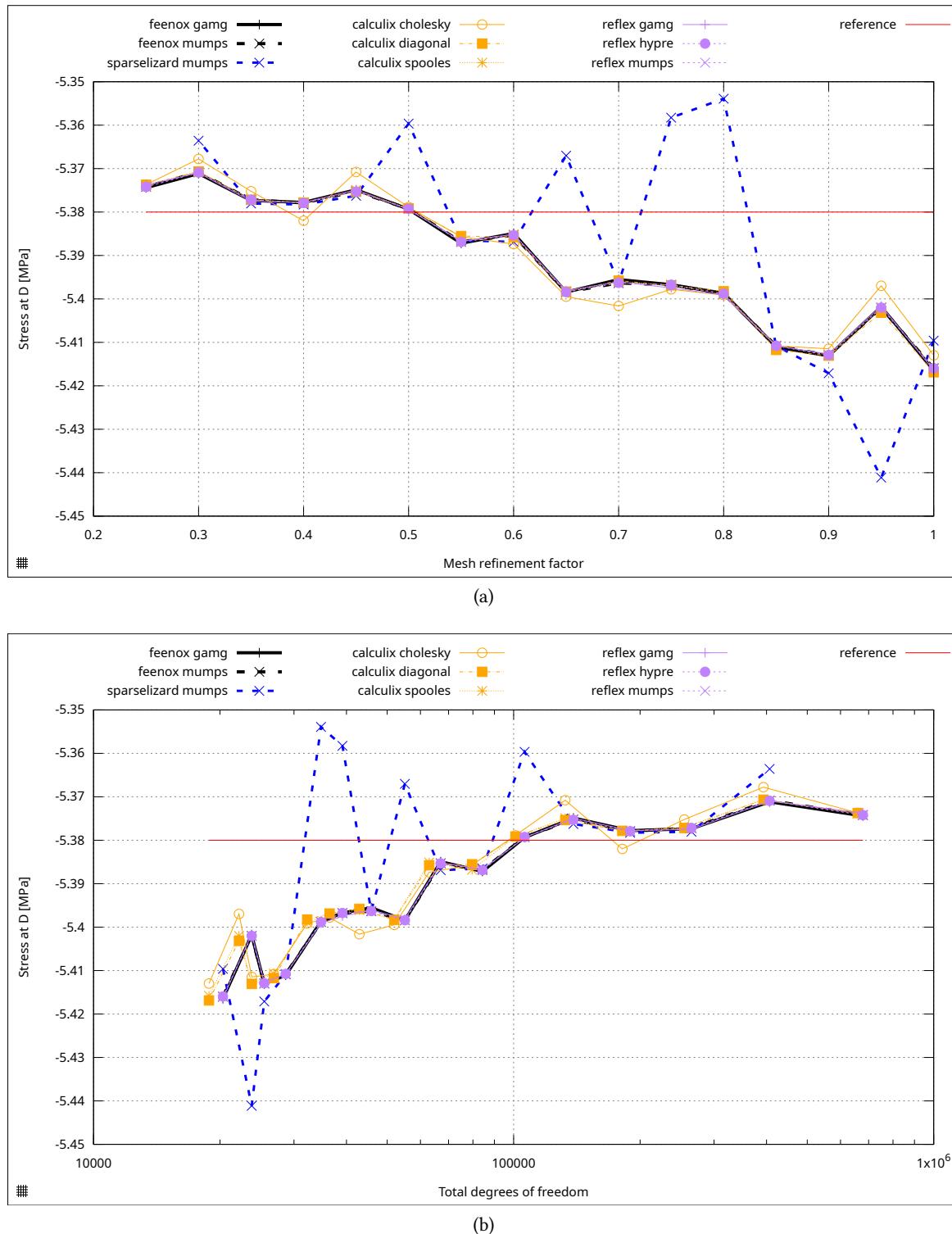


Figure 3: Stress

Parametric NAFEMS LE10 benchmark with tet elements

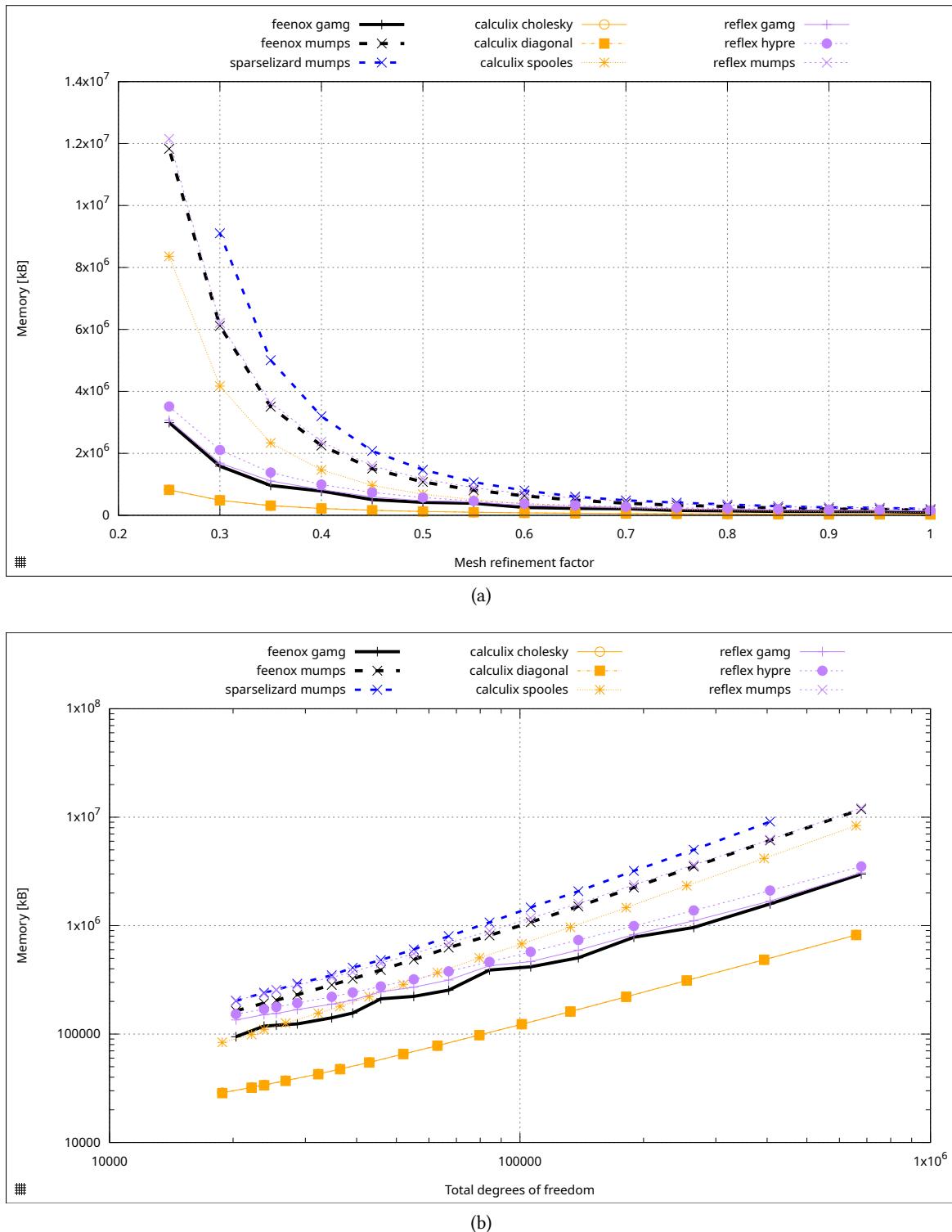


Figure 4: Memory

Parametric NAFEMS LE10 benchmark with tet elements

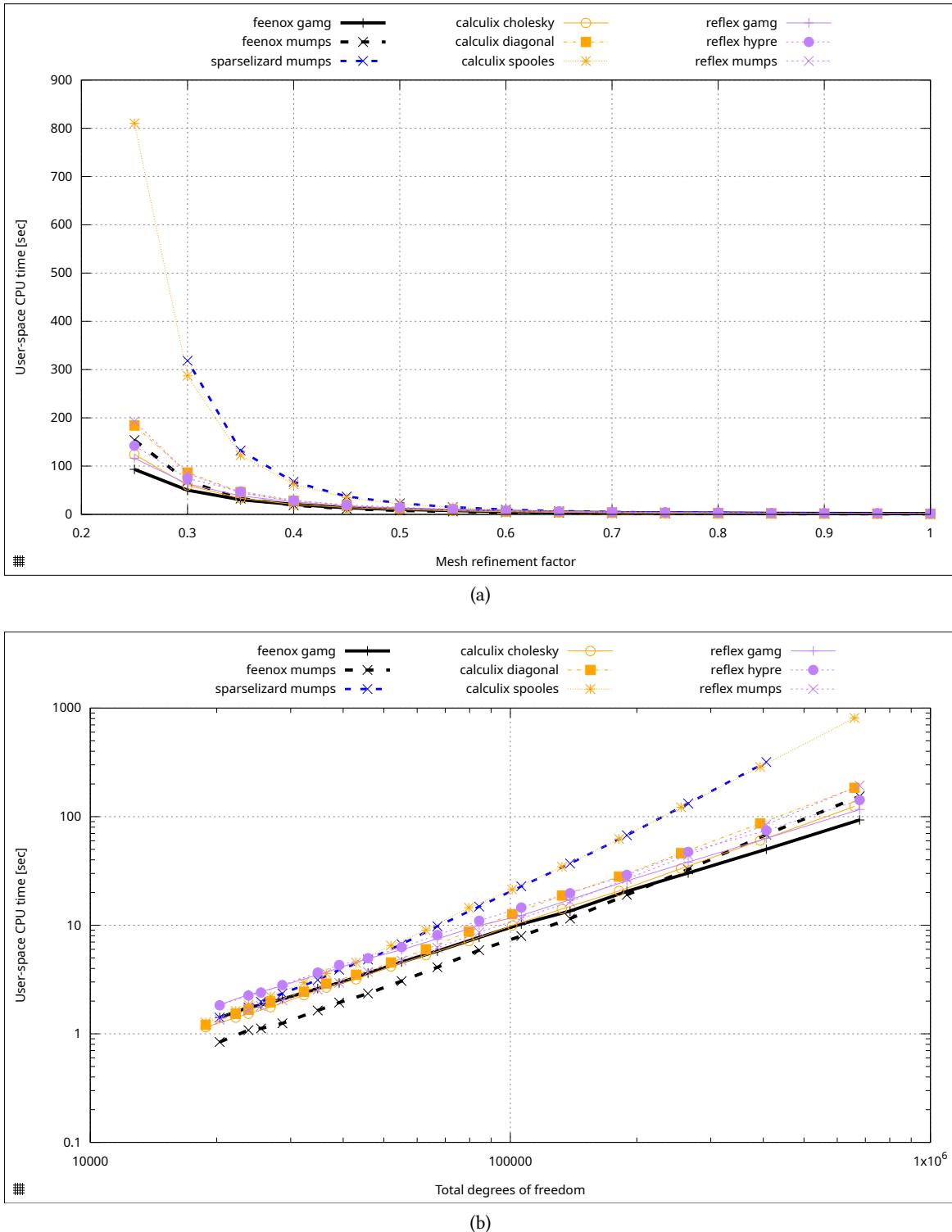


Figure 5: User

Parametric NAFEMS LE10 benchmark with tet elements

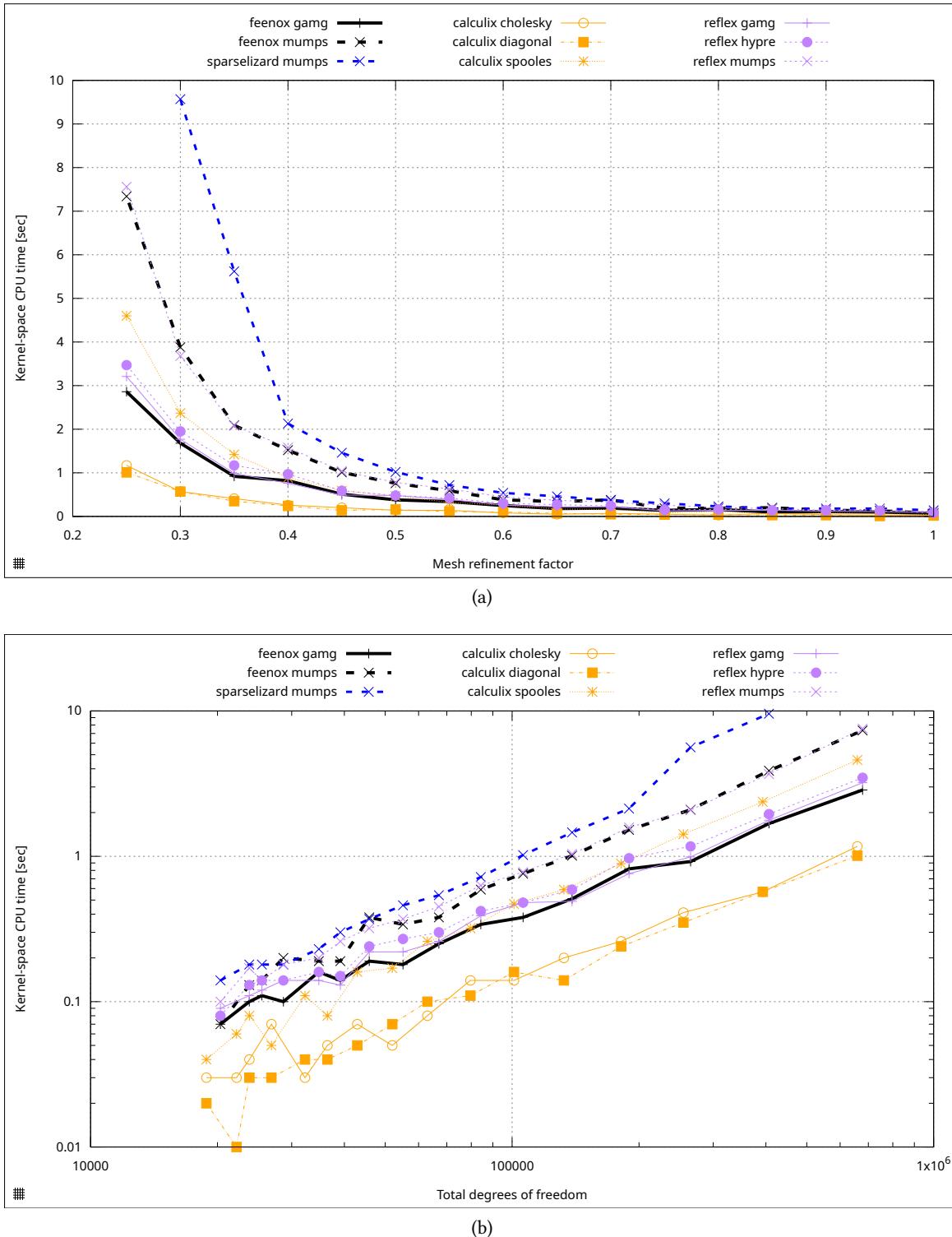


Figure 6: kernel

5 Tables

5.1 $c = 1$

 Table 2: $c = 1$ sorted by wall time

| Program | Solver | DOFs | σ_y | Wall [s] | Kernel [s] | User [s] | Memory [Gb] |
|-------------|----------|--------|------------|----------|------------|----------|-------------|
| feenox | mumps | 20,325 | -5.416 | 1.1 | 0.1 | 0.8 | 0.16 |
| calculix | cholesky | 18,824 | -5.413 | 1.2 | 0.0 | 1.1 | 0.03 |
| calculix | diagonal | 18,824 | -5.417 | 1.2 | 0.0 | 1.2 | 0.03 |
| calculix | spooles | 18,824 | -5.416 | 1.3 | 0.0 | 1.3 | 0.08 |
| sparselizar | mumps | 20,325 | -5.410 | 1.4 | 0.1 | 1.4 | 0.19 |
| reflex | mumps | 20,325 | -5.416 | 1.6 | 0.1 | 1.3 | 0.19 |
| feenox | gamg | 20,325 | -5.416 | 1.7 | 0.1 | 1.4 | 0.09 |
| reflex | gamg | 20,325 | -5.416 | 2.1 | 0.1 | 1.9 | 0.13 |
| reflex | hypre | 20,325 | -5.416 | 2.1 | 0.1 | 1.8 | 0.15 |

 Table 3: $c = 1$ sorted by memory

| Program | Solver | DOFs | σ_y | Wall [s] | Kernel [s] | User [s] | Memory [Gb] |
|-------------|----------|--------|------------|----------|------------|----------|-------------|
| calculix | cholesky | 18,824 | -5.413 | 1.2 | 0.0 | 1.1 | 0.03 |
| calculix | diagonal | 18,824 | -5.417 | 1.2 | 0.0 | 1.2 | 0.03 |
| calculix | spooles | 18,824 | -5.416 | 1.3 | 0.0 | 1.3 | 0.08 |
| feenox | gamg | 20,325 | -5.416 | 1.7 | 0.1 | 1.4 | 0.09 |
| reflex | gamg | 20,325 | -5.416 | 2.1 | 0.1 | 1.9 | 0.13 |
| reflex | hypre | 20,325 | -5.416 | 2.1 | 0.1 | 1.8 | 0.15 |
| feenox | mumps | 20,325 | -5.416 | 1.1 | 0.1 | 0.8 | 0.16 |
| reflex | mumps | 20,325 | -5.416 | 1.6 | 0.1 | 1.3 | 0.19 |
| sparselizar | mumps | 20,325 | -5.410 | 1.4 | 0.1 | 1.4 | 0.19 |

5.2 $c = 0.95$

 Table 4: $c = 0.95$ sorted by wall time

| Program | Solver | DOFs | σ_y | Wall [s] | Kernel [s] | User [s] | Memory [Gb] |
|-------------|----------|--------|------------|----------|------------|----------|-------------|
| calculix | cholesky | 22,194 | -5.397 | 1.4 | 0.0 | 1.4 | 0.03 |
| feenox | mumps | 23,793 | -5.402 | 1.4 | 0.1 | 1.1 | 0.18 |
| calculix | diagonal | 22,194 | -5.403 | 1.6 | 0.0 | 1.5 | 0.03 |
| calculix | spooles | 22,194 | -5.402 | 1.7 | 0.1 | 1.6 | 0.09 |
| sparselizar | mumps | 23,793 | -5.441 | 1.8 | 0.2 | 1.8 | 0.23 |
| feenox | gamg | 23,793 | -5.402 | 2.0 | 0.1 | 1.8 | 0.11 |
| reflex | mumps | 23,793 | -5.402 | 2.0 | 0.2 | 1.6 | 0.22 |

Parametric NAFEMS LE10 benchmark with tet elements

| Program | Solver | DOFs | σ_y | Wall [s] | Kernel [s] | User [s] | Memory [Gb] |
|---------|--------|--------|------------|----------|------------|----------|-------------|
| reflex | gamg | 23,793 | -5.402 | 2.6 | 0.1 | 2.3 | 0.14 |
| reflex | hypre | 23,793 | -5.402 | 2.6 | 0.1 | 2.2 | 0.16 |

Table 5: $c = 0.95$ sorted by memory

| Program | Solver | DOFs | σ_y | Wall [s] | Kernel [s] | User [s] | Memory [Gb] |
|-------------|----------|--------|------------|----------|------------|----------|-------------|
| calculix | cholesky | 22,194 | -5.397 | 1.4 | 0.0 | 1.4 | 0.03 |
| calculix | diagonal | 22,194 | -5.403 | 1.6 | 0.0 | 1.5 | 0.03 |
| calculix | spooles | 22,194 | -5.402 | 1.7 | 0.1 | 1.6 | 0.09 |
| feenox | gamg | 23,793 | -5.402 | 2.0 | 0.1 | 1.8 | 0.11 |
| reflex | gamg | 23,793 | -5.402 | 2.6 | 0.1 | 2.3 | 0.14 |
| reflex | hypre | 23,793 | -5.402 | 2.6 | 0.1 | 2.2 | 0.16 |
| feenox | mumps | 23,793 | -5.402 | 1.4 | 0.1 | 1.1 | 0.18 |
| reflex | mumps | 23,793 | -5.402 | 2.0 | 0.2 | 1.6 | 0.22 |
| sparselizar | mumps | 23,793 | -5.441 | 1.8 | 0.2 | 1.8 | 0.23 |

5.3 $c = 0.9$

Table 6: $c = 0.9$ sorted by wall time

| Program | Solver | DOFs | σ_y | Wall [s] | Kernel [s] | User [s] | Memory [Gb] |
|-------------|----------|--------|------------|----------|------------|----------|-------------|
| feenox | mumps | 25,491 | -5.413 | 1.5 | 0.1 | 1.1 | 0.20 |
| calculix | cholesky | 23,808 | -5.411 | 1.6 | 0.0 | 1.5 | 0.03 |
| calculix | diagonal | 23,808 | -5.413 | 1.7 | 0.0 | 1.7 | 0.03 |
| calculix | spooles | 23,808 | -5.413 | 1.9 | 0.1 | 1.9 | 0.11 |
| sparselizar | mumps | 25,491 | -5.417 | 2.0 | 0.2 | 2.0 | 0.24 |
| feenox | gamg | 25,491 | -5.413 | 2.1 | 0.1 | 1.8 | 0.11 |
| reflex | mumps | 25,491 | -5.413 | 2.1 | 0.1 | 1.8 | 0.24 |
| reflex | gamg | 25,491 | -5.413 | 2.7 | 0.1 | 2.4 | 0.15 |
| reflex | hypre | 25,491 | -5.413 | 2.7 | 0.1 | 2.4 | 0.17 |

Table 7: $c = 0.9$ sorted by memory

| Program | Solver | DOFs | σ_y | Wall [s] | Kernel [s] | User [s] | Memory [Gb] |
|----------|----------|--------|------------|----------|------------|----------|-------------|
| calculix | cholesky | 23,808 | -5.411 | 1.6 | 0.0 | 1.5 | 0.03 |
| calculix | diagonal | 23,808 | -5.413 | 1.7 | 0.0 | 1.7 | 0.03 |
| calculix | spooles | 23,808 | -5.413 | 1.9 | 0.1 | 1.9 | 0.11 |
| feenox | gamg | 25,491 | -5.413 | 2.1 | 0.1 | 1.8 | 0.11 |
| reflex | gamg | 25,491 | -5.413 | 2.7 | 0.1 | 2.4 | 0.15 |

Parametric NAFEMS LE10 benchmark with tet elements

| Program | Solver | DOFs | σ_y | Wall [s] | Kernel [s] | User [s] | Memory [Gb] |
|-------------|--------|--------|------------|----------|------------|----------|-------------|
| reflex | hypre | 25,491 | -5.413 | 2.7 | 0.1 | 2.4 | 0.17 |
| feenox | mumps | 25,491 | -5.413 | 1.5 | 0.1 | 1.1 | 0.20 |
| reflex | mumps | 25,491 | -5.413 | 2.1 | 0.1 | 1.8 | 0.24 |
| sparselizar | mumps | 25,491 | -5.417 | 2.0 | 0.2 | 2.0 | 0.24 |

5.4 $c = 0.85$

Table 8: $c = 0.85$ sorted by wall time

| Program | Solver | DOFs | σ_y | Wall [s] | Kernel [s] | User [s] | Memory [Gb] |
|-------------|----------|--------|------------|----------|------------|----------|-------------|
| feenox | mumps | 28,668 | -5.411 | 1.6 | 0.2 | 1.2 | 0.22 |
| calculix | cholesky | 26,855 | -5.411 | 1.8 | 0.1 | 1.8 | 0.04 |
| calculix | diagonal | 26,855 | -5.412 | 2.0 | 0.0 | 1.9 | 0.04 |
| calculix | spooles | 26,855 | -5.411 | 2.3 | 0.1 | 2.2 | 0.12 |
| feenox | gamg | 28,668 | -5.411 | 2.4 | 0.1 | 2.1 | 0.12 |
| reflex | mumps | 28,668 | -5.411 | 2.4 | 0.2 | 2.0 | 0.27 |
| sparselizar | mumps | 28,668 | -5.411 | 2.4 | 0.2 | 2.4 | 0.28 |
| reflex | gamg | 28,668 | -5.411 | 3.1 | 0.1 | 2.8 | 0.16 |
| reflex | hypre | 28,668 | -5.411 | 3.1 | 0.1 | 2.8 | 0.18 |

Table 9: $c = 0.85$ sorted by memory

| Program | Solver | DOFs | σ_y | Wall [s] | Kernel [s] | User [s] | Memory [Gb] |
|-------------|----------|--------|------------|----------|------------|----------|-------------|
| calculix | cholesky | 26,855 | -5.411 | 1.8 | 0.1 | 1.8 | 0.04 |
| calculix | diagonal | 26,855 | -5.412 | 2.0 | 0.0 | 1.9 | 0.04 |
| calculix | spooles | 26,855 | -5.411 | 2.3 | 0.1 | 2.2 | 0.12 |
| feenox | gamg | 28,668 | -5.411 | 2.4 | 0.1 | 2.1 | 0.12 |
| reflex | gamg | 28,668 | -5.411 | 3.1 | 0.1 | 2.8 | 0.16 |
| reflex | hypre | 28,668 | -5.411 | 3.1 | 0.1 | 2.8 | 0.18 |
| feenox | mumps | 28,668 | -5.411 | 1.6 | 0.2 | 1.2 | 0.22 |
| reflex | mumps | 28,668 | -5.411 | 2.4 | 0.2 | 2.0 | 0.27 |
| sparselizar | mumps | 28,668 | -5.411 | 2.4 | 0.2 | 2.4 | 0.28 |

5.5 $c = 0.8$

Table 10: $c = 0.8$ sorted by wall time

| Program | Solver | DOFs | σ_y | Wall [s] | Kernel [s] | User [s] | Memory [Gb] |
|---------|--------|--------|------------|----------|------------|----------|-------------|
| feenox | mumps | 34,788 | -5.399 | 2.0 | 0.2 | 1.6 | 0.27 |

Parametric NAFEMS LE10 benchmark with tet elements

| Program | Solver | DOFs | σ_y | Wall [s] | Kernel [s] | User [s] | Memory [Gb] |
|-------------|----------|--------|------------|----------|------------|----------|-------------|
| calculix | cholesky | 32,255 | -5.399 | 2.3 | 0.0 | 2.3 | 0.04 |
| calculix | diagonal | 32,255 | -5.398 | 2.5 | 0.0 | 2.4 | 0.04 |
| feenox | gamg | 34,788 | -5.399 | 3.0 | 0.2 | 2.6 | 0.13 |
| reflex | mumps | 34,788 | -5.399 | 3.0 | 0.2 | 2.5 | 0.32 |
| calculix | spooles | 32,255 | -5.399 | 3.1 | 0.1 | 3.0 | 0.15 |
| sparselizar | mumps | 34,788 | -5.354 | 3.2 | 0.2 | 3.1 | 0.33 |
| reflex | gamg | 34,788 | -5.399 | 3.8 | 0.1 | 3.5 | 0.18 |
| reflex | hypre | 34,788 | -5.399 | 4.0 | 0.2 | 3.7 | 0.21 |

Table 11: $c = 0.8$ sorted by memory

| Program | Solver | DOFs | σ_y | Wall [s] | Kernel [s] | User [s] | Memory [Gb] |
|-------------|----------|--------|------------|----------|------------|----------|-------------|
| calculix | cholesky | 32,255 | -5.399 | 2.3 | 0.0 | 2.3 | 0.04 |
| calculix | diagonal | 32,255 | -5.398 | 2.5 | 0.0 | 2.4 | 0.04 |
| feenox | gamg | 34,788 | -5.399 | 3.0 | 0.2 | 2.6 | 0.13 |
| calculix | spooles | 32,255 | -5.399 | 3.1 | 0.1 | 3.0 | 0.15 |
| reflex | gamg | 34,788 | -5.399 | 3.8 | 0.1 | 3.5 | 0.18 |
| reflex | hypre | 34,788 | -5.399 | 4.0 | 0.2 | 3.7 | 0.21 |
| feenox | mumps | 34,788 | -5.399 | 2.0 | 0.2 | 1.6 | 0.27 |
| reflex | mumps | 34,788 | -5.399 | 3.0 | 0.2 | 2.5 | 0.32 |
| sparselizar | mumps | 34,788 | -5.354 | 3.2 | 0.2 | 3.1 | 0.33 |

5.6 $c = 0.75$

Table 12: $c = 0.75$ sorted by wall time

| Program | Solver | DOFs | σ_y | Wall [s] | Kernel [s] | User [s] | Memory [Gb] |
|-------------|----------|--------|------------|----------|------------|----------|-------------|
| feenox | mumps | 39,129 | -5.397 | 2.3 | 0.2 | 1.9 | 0.31 |
| calculix | cholesky | 36,462 | -5.398 | 2.7 | 0.1 | 2.7 | 0.05 |
| calculix | diagonal | 36,462 | -5.397 | 2.9 | 0.0 | 2.9 | 0.05 |
| feenox | gamg | 39,129 | -5.397 | 3.3 | 0.1 | 2.9 | 0.15 |
| reflex | mumps | 39,129 | -5.397 | 3.4 | 0.3 | 3.0 | 0.36 |
| calculix | spooles | 36,462 | -5.397 | 3.7 | 0.1 | 3.6 | 0.17 |
| sparselizar | mumps | 39,129 | -5.358 | 4.0 | 0.3 | 3.9 | 0.39 |
| reflex | gamg | 39,129 | -5.397 | 4.4 | 0.1 | 4.1 | 0.20 |
| reflex | hypre | 39,129 | -5.397 | 4.7 | 0.1 | 4.3 | 0.23 |

Parametric NAFEMS LE10 benchmark with tet elements

Table 13: $c = 0.75$ sorted by memory

| Program | Solver | DOFs | σ_y | Wall [s] | Kernel [s] | User [s] | Memory [Gb] |
|-------------|----------|--------|------------|----------|------------|----------|-------------|
| calculix | cholesky | 36,462 | -5.398 | 2.7 | 0.1 | 2.7 | 0.05 |
| calculix | diagonal | 36,462 | -5.397 | 2.9 | 0.0 | 2.9 | 0.05 |
| feenox | gamg | 39,129 | -5.397 | 3.3 | 0.1 | 2.9 | 0.15 |
| calculix | spooles | 36,462 | -5.397 | 3.7 | 0.1 | 3.6 | 0.17 |
| reflex | gamg | 39,129 | -5.397 | 4.4 | 0.1 | 4.1 | 0.20 |
| reflex | hypre | 39,129 | -5.397 | 4.7 | 0.1 | 4.3 | 0.23 |
| feenox | mumps | 39,129 | -5.397 | 2.3 | 0.2 | 1.9 | 0.31 |
| reflex | mumps | 39,129 | -5.397 | 3.4 | 0.3 | 3.0 | 0.36 |
| sparselizar | mumps | 39,129 | -5.358 | 4.0 | 0.3 | 3.9 | 0.39 |

5.7 $c = 0.7$

Table 14: $c = 0.7$ sorted by wall time

| Program | Solver | DOFs | σ_y | Wall [s] | Kernel [s] | User [s] | Memory [Gb] |
|-------------|----------|--------|------------|----------|------------|----------|-------------|
| feenox | mumps | 45,822 | -5.396 | 2.9 | 0.4 | 2.4 | 0.37 |
| calculix | cholesky | 42,928 | -5.402 | 3.2 | 0.1 | 3.2 | 0.05 |
| calculix | diagonal | 42,928 | -5.396 | 3.5 | 0.1 | 3.5 | 0.05 |
| feenox | gamg | 45,822 | -5.396 | 4.0 | 0.2 | 3.6 | 0.20 |
| reflex | mumps | 45,822 | -5.396 | 4.2 | 0.3 | 3.7 | 0.43 |
| calculix | spooles | 42,928 | -5.396 | 4.7 | 0.2 | 4.5 | 0.21 |
| sparselizar | mumps | 45,822 | -5.396 | 5.0 | 0.4 | 4.8 | 0.46 |
| reflex | gamg | 45,822 | -5.396 | 5.3 | 0.2 | 4.9 | 0.23 |
| reflex | hypre | 45,822 | -5.396 | 5.4 | 0.2 | 5.0 | 0.26 |

Table 15: $c = 0.7$ sorted by memory

| Program | Solver | DOFs | σ_y | Wall [s] | Kernel [s] | User [s] | Memory [Gb] |
|-------------|----------|--------|------------|----------|------------|----------|-------------|
| calculix | cholesky | 42,928 | -5.402 | 3.2 | 0.1 | 3.2 | 0.05 |
| calculix | diagonal | 42,928 | -5.396 | 3.5 | 0.1 | 3.5 | 0.05 |
| feenox | gamg | 45,822 | -5.396 | 4.0 | 0.2 | 3.6 | 0.20 |
| calculix | spooles | 42,928 | -5.396 | 4.7 | 0.2 | 4.5 | 0.21 |
| reflex | gamg | 45,822 | -5.396 | 5.3 | 0.2 | 4.9 | 0.23 |
| reflex | hypre | 45,822 | -5.396 | 5.4 | 0.2 | 5.0 | 0.26 |
| feenox | mumps | 45,822 | -5.396 | 2.9 | 0.4 | 2.4 | 0.37 |
| reflex | mumps | 45,822 | -5.396 | 4.2 | 0.3 | 3.7 | 0.43 |
| sparselizar | mumps | 45,822 | -5.396 | 5.0 | 0.4 | 4.8 | 0.46 |

Parametric NAFEMS LE10 benchmark with tet elements

5.8 $c = 0.65$

Table 16: $c = 0.65$ sorted by wall time

| Program | Solver | DOFs | σ_y | Wall [s] | Kernel [s] | User [s] | Memory [Gb] |
|-------------|----------|--------|------------|----------|------------|----------|-------------|
| feenox | mumps | 55,098 | -5.398 | 3.6 | 0.3 | 3.1 | 0.46 |
| calculix | cholesky | 51,971 | -5.399 | 4.2 | 0.1 | 4.2 | 0.06 |
| calculix | diagonal | 51,971 | -5.398 | 4.6 | 0.1 | 4.5 | 0.06 |
| feenox | gamg | 55,098 | -5.398 | 5.0 | 0.2 | 4.6 | 0.21 |
| reflex | mumps | 55,098 | -5.398 | 5.3 | 0.4 | 4.7 | 0.53 |
| reflex | gamg | 55,098 | -5.398 | 6.4 | 0.2 | 5.9 | 0.26 |
| calculix | spooles | 51,971 | -5.398 | 6.7 | 0.2 | 6.5 | 0.27 |
| reflex | hypre | 55,098 | -5.398 | 6.8 | 0.3 | 6.3 | 0.30 |
| sparselizar | mumps | 55,098 | -5.367 | 6.8 | 0.5 | 6.7 | 0.58 |

Table 17: $c = 0.65$ sorted by memory

| Program | Solver | DOFs | σ_y | Wall [s] | Kernel [s] | User [s] | Memory [Gb] |
|-------------|----------|--------|------------|----------|------------|----------|-------------|
| calculix | cholesky | 51,971 | -5.399 | 4.2 | 0.1 | 4.2 | 0.06 |
| calculix | diagonal | 51,971 | -5.398 | 4.6 | 0.1 | 4.5 | 0.06 |
| feenox | gamg | 55,098 | -5.398 | 5.0 | 0.2 | 4.6 | 0.21 |
| reflex | gamg | 55,098 | -5.398 | 6.4 | 0.2 | 5.9 | 0.26 |
| calculix | spooles | 51,971 | -5.398 | 6.7 | 0.2 | 6.5 | 0.27 |
| reflex | hypre | 55,098 | -5.398 | 6.8 | 0.3 | 6.3 | 0.30 |
| feenox | mumps | 55,098 | -5.398 | 3.6 | 0.3 | 3.1 | 0.46 |
| reflex | mumps | 55,098 | -5.398 | 5.3 | 0.4 | 4.7 | 0.53 |
| sparselizar | mumps | 55,098 | -5.367 | 6.8 | 0.5 | 6.7 | 0.58 |

5.9 $c = 0.6$

Table 18: $c = 0.6$ sorted by wall time

| Program | Solver | DOFs | σ_y | Wall [s] | Kernel [s] | User [s] | Memory [Gb] |
|----------|----------|--------|------------|----------|------------|----------|-------------|
| feenox | mumps | 67,038 | -5.385 | 4.7 | 0.4 | 4.1 | 0.60 |
| calculix | cholesky | 62,943 | -5.387 | 5.4 | 0.1 | 5.3 | 0.07 |
| calculix | diagonal | 62,943 | -5.386 | 6.1 | 0.1 | 6.0 | 0.07 |
| feenox | gamg | 67,038 | -5.385 | 6.2 | 0.2 | 5.8 | 0.24 |
| reflex | mumps | 67,038 | -5.385 | 6.9 | 0.5 | 6.2 | 0.66 |
| reflex | gamg | 67,038 | -5.385 | 7.9 | 0.3 | 7.5 | 0.30 |
| reflex | hypre | 67,038 | -5.385 | 8.6 | 0.3 | 8.1 | 0.36 |
| calculix | spooles | 62,943 | -5.385 | 9.3 | 0.3 | 9.0 | 0.35 |

Parametric NAFEMS LE10 benchmark with tet elements

| Program | Solver | DOFs | σ_y | Wall [s] | Kernel [s] | User [s] | Memory [Gb] |
|-------------|--------|--------|------------|----------|------------|----------|-------------|
| sparselizar | mumps | 67,038 | -5.387 | 9.9 | 0.5 | 9.8 | 0.76 |

Table 19: $c = 0.6$ sorted by memory

| Program | Solver | DOFs | σ_y | Wall [s] | Kernel [s] | User [s] | Memory [Gb] |
|-------------|----------|--------|------------|----------|------------|----------|-------------|
| calculix | cholesky | 62,943 | -5.387 | 5.4 | 0.1 | 5.3 | 0.07 |
| calculix | diagonal | 62,943 | -5.386 | 6.1 | 0.1 | 6.0 | 0.07 |
| feenox | gamg | 67,038 | -5.385 | 6.2 | 0.2 | 5.8 | 0.24 |
| reflex | gamg | 67,038 | -5.385 | 7.9 | 0.3 | 7.5 | 0.30 |
| calculix | spooles | 62,943 | -5.385 | 9.3 | 0.3 | 9.0 | 0.35 |
| reflex | hypre | 67,038 | -5.385 | 8.6 | 0.3 | 8.1 | 0.36 |
| feenox | mumps | 67,038 | -5.385 | 4.7 | 0.4 | 4.1 | 0.60 |
| reflex | mumps | 67,038 | -5.385 | 6.9 | 0.5 | 6.2 | 0.66 |
| sparselizar | mumps | 67,038 | -5.387 | 9.9 | 0.5 | 9.8 | 0.76 |

5.10 $c = 0.55$

Table 20: $c = 0.55$ sorted by wall time

| Program | Solver | DOFs | σ_y | Wall [s] | Kernel [s] | User [s] | Memory [Gb] |
|-------------|----------|--------|------------|----------|------------|----------|-------------|
| feenox | mumps | 84,288 | -5.387 | 6.7 | 0.6 | 5.9 | 0.77 |
| calculix | cholesky | 79,636 | -5.386 | 7.3 | 0.1 | 7.1 | 0.09 |
| feenox | gamg | 84,288 | -5.387 | 8.3 | 0.3 | 7.7 | 0.37 |
| calculix | diagonal | 79,636 | -5.386 | 8.9 | 0.1 | 8.8 | 0.09 |
| reflex | mumps | 84,288 | -5.387 | 9.4 | 0.6 | 8.6 | 0.85 |
| reflex | gamg | 84,288 | -5.387 | 10.5 | 0.4 | 9.9 | 0.41 |
| reflex | hypre | 84,288 | -5.387 | 11.6 | 0.4 | 11.0 | 0.44 |
| calculix | spooles | 79,636 | -5.387 | 14.8 | 0.3 | 14.5 | 0.48 |
| sparselizar | mumps | 84,288 | -5.386 | 15.1 | 0.7 | 14.8 | 1.02 |

Table 21: $c = 0.55$ sorted by memory

| Program | Solver | DOFs | σ_y | Wall [s] | Kernel [s] | User [s] | Memory [Gb] |
|----------|----------|--------|------------|----------|------------|----------|-------------|
| calculix | cholesky | 79,636 | -5.386 | 7.3 | 0.1 | 7.1 | 0.09 |
| calculix | diagonal | 79,636 | -5.386 | 8.9 | 0.1 | 8.8 | 0.09 |
| feenox | gamg | 84,288 | -5.387 | 8.3 | 0.3 | 7.7 | 0.37 |
| reflex | gamg | 84,288 | -5.387 | 10.5 | 0.4 | 9.9 | 0.41 |
| reflex | hypre | 84,288 | -5.387 | 11.6 | 0.4 | 11.0 | 0.44 |
| calculix | spooles | 79,636 | -5.387 | 14.8 | 0.3 | 14.5 | 0.48 |

Parametric NAFEMS LE10 benchmark with tet elements

| Program | Solver | DOFs | σ_y | Wall [s] | Kernel [s] | User [s] | Memory [Gb] |
|-------------|--------|--------|------------|----------|------------|----------|-------------|
| feenox | mumps | 84,288 | -5.387 | 6.7 | 0.6 | 5.9 | 0.77 |
| reflex | mumps | 84,288 | -5.387 | 9.4 | 0.6 | 8.6 | 0.85 |
| sparselizar | mumps | 84,288 | -5.386 | 15.1 | 0.7 | 14.8 | 1.02 |

5.11 $c = 0.5$

Table 22: $c = 0.5$ sorted by wall time

| Program | Solver | DOFs | σ_y | Wall [s] | Kernel [s] | User [s] | Memory [Gb] |
|-------------|----------|---------|------------|----------|------------|----------|-------------|
| feenox | mumps | 106,185 | -5.379 | 8.9 | 0.8 | 8.0 | 1.02 |
| calculix | cholesky | 101,014 | -5.379 | 10.1 | 0.1 | 9.9 | 0.12 |
| feenox | gamg | 106,185 | -5.379 | 10.8 | 0.4 | 10.2 | 0.40 |
| reflex | mumps | 106,185 | -5.379 | 12.5 | 0.8 | 11.6 | 1.12 |
| calculix | diagonal | 101,014 | -5.379 | 12.8 | 0.2 | 12.6 | 0.12 |
| reflex | gamg | 106,185 | -5.379 | 13.0 | 0.5 | 12.3 | 0.44 |
| reflex | hypre | 106,185 | -5.379 | 15.2 | 0.5 | 14.6 | 0.55 |
| calculix | spooles | 101,014 | -5.379 | 21.8 | 0.5 | 21.3 | 0.65 |
| sparselizar | mumps | 106,185 | -5.360 | 23.2 | 1.0 | 22.8 | 1.40 |

Table 23: $c = 0.5$ sorted by memory

| Program | Solver | DOFs | σ_y | Wall [s] | Kernel [s] | User [s] | Memory [Gb] |
|-------------|----------|---------|------------|----------|------------|----------|-------------|
| calculix | cholesky | 101,014 | -5.379 | 10.1 | 0.1 | 9.9 | 0.12 |
| calculix | diagonal | 101,014 | -5.379 | 12.8 | 0.2 | 12.6 | 0.12 |
| feenox | gamg | 106,185 | -5.379 | 10.8 | 0.4 | 10.2 | 0.40 |
| reflex | gamg | 106,185 | -5.379 | 13.0 | 0.5 | 12.3 | 0.44 |
| reflex | hypre | 106,185 | -5.379 | 15.2 | 0.5 | 14.6 | 0.55 |
| calculix | spooles | 101,014 | -5.379 | 21.8 | 0.5 | 21.3 | 0.65 |
| feenox | mumps | 106,185 | -5.379 | 8.9 | 0.8 | 8.0 | 1.02 |
| reflex | mumps | 106,185 | -5.379 | 12.5 | 0.8 | 11.6 | 1.12 |
| sparselizar | mumps | 106,185 | -5.360 | 23.2 | 1.0 | 22.8 | 1.40 |

5.12 $c = 0.45$

Table 24: $c = 0.45$ sorted by wall time

| Program | Solver | DOFs | σ_y | Wall [s] | Kernel [s] | User [s] | Memory [Gb] |
|---------|--------|---------|------------|----------|------------|----------|-------------|
| feenox | mumps | 138,741 | -5.375 | 12.7 | 1.0 | 11.5 | 1.44 |
| feenox | gamg | 138,741 | -5.375 | 14.2 | 0.5 | 13.5 | 0.48 |

Parametric NAFEMS LE10 benchmark with tet elements

| Program | Solver | DOFs | σ_y | Wall [s] | Kernel [s] | User [s] | Memory [Gb] |
|-------------|----------|---------|------------|----------|------------|----------|-------------|
| calculix | cholesky | 132,696 | -5.371 | 14.3 | 0.2 | 14.1 | 0.15 |
| reflex | mumps | 138,741 | -5.375 | 17.7 | 1.0 | 16.5 | 1.52 |
| reflex | gamg | 138,741 | -5.375 | 17.9 | 0.5 | 17.2 | 0.57 |
| calculix | diagonal | 132,696 | -5.375 | 18.9 | 0.1 | 18.8 | 0.15 |
| reflex | hypre | 138,741 | -5.375 | 20.5 | 0.6 | 19.7 | 0.70 |
| calculix | spooles | 132,696 | -5.375 | 35.2 | 0.6 | 34.6 | 0.92 |
| sparselizar | mumps | 138,741 | -5.376 | 37.6 | 1.5 | 37.0 | 1.98 |

Table 25: $c = 0.45$ sorted by memory

| Program | Solver | DOFs | σ_y | Wall [s] | Kernel [s] | User [s] | Memory [Gb] |
|-------------|----------|---------|------------|----------|------------|----------|-------------|
| calculix | cholesky | 132,696 | -5.371 | 14.3 | 0.2 | 14.1 | 0.15 |
| calculix | diagonal | 132,696 | -5.375 | 18.9 | 0.1 | 18.8 | 0.15 |
| feenox | gamg | 138,741 | -5.375 | 14.2 | 0.5 | 13.5 | 0.48 |
| reflex | gamg | 138,741 | -5.375 | 17.9 | 0.5 | 17.2 | 0.57 |
| reflex | hypre | 138,741 | -5.375 | 20.5 | 0.6 | 19.7 | 0.70 |
| calculix | spooles | 132,696 | -5.375 | 35.2 | 0.6 | 34.6 | 0.92 |
| feenox | mumps | 138,741 | -5.375 | 12.7 | 1.0 | 11.5 | 1.44 |
| reflex | mumps | 138,741 | -5.375 | 17.7 | 1.0 | 16.5 | 1.52 |
| sparselizar | mumps | 138,741 | -5.376 | 37.6 | 1.5 | 37.0 | 1.98 |

5.13 $c = 0.4$

Table 26: $c = 0.4$ sorted by wall time

| Program | Solver | DOFs | σ_y | Wall [s] | Kernel [s] | User [s] | Memory [Gb] |
|-------------|----------|---------|------------|----------|------------|----------|-------------|
| feenox | mumps | 189,408 | -5.378 | 20.8 | 1.5 | 19.1 | 2.15 |
| calculix | cholesky | 181,449 | -5.382 | 20.9 | 0.3 | 20.7 | 0.21 |
| feenox | gamg | 189,408 | -5.378 | 21.5 | 0.8 | 20.5 | 0.75 |
| reflex | gamg | 189,408 | -5.378 | 26.6 | 0.8 | 25.6 | 0.79 |
| calculix | diagonal | 181,449 | -5.378 | 28.3 | 0.2 | 28.1 | 0.21 |
| reflex | mumps | 189,408 | -5.378 | 28.5 | 1.6 | 26.7 | 2.27 |
| reflex | hypre | 189,408 | -5.378 | 30.2 | 1.0 | 29.1 | 0.95 |
| calculix | spooles | 181,449 | -5.378 | 63.3 | 0.9 | 62.4 | 1.40 |
| sparselizar | mumps | 189,408 | -5.378 | 68.3 | 2.1 | 67.4 | 3.05 |

Parametric NAFEMS LE10 benchmark with tet elements

Table 27: $c = 0.4$ sorted by memory

| Program | Solver | DOFs | σ_y | Wall [s] | Kernel [s] | User [s] | Memory [Gb] |
|-------------|----------|---------|------------|----------|------------|----------|-------------|
| calculix | cholesky | 181,449 | -5.382 | 20.9 | 0.3 | 20.7 | 0.21 |
| calculix | diagonal | 181,449 | -5.378 | 28.3 | 0.2 | 28.1 | 0.21 |
| feenox | gamg | 189,408 | -5.378 | 21.5 | 0.8 | 20.5 | 0.75 |
| reflex | gamg | 189,408 | -5.378 | 26.6 | 0.8 | 25.6 | 0.79 |
| reflex | hypre | 189,408 | -5.378 | 30.2 | 1.0 | 29.1 | 0.95 |
| calculix | spooles | 181,449 | -5.378 | 63.3 | 0.9 | 62.4 | 1.40 |
| feenox | mumps | 189,408 | -5.378 | 20.8 | 1.5 | 19.1 | 2.15 |
| reflex | mumps | 189,408 | -5.378 | 28.5 | 1.6 | 26.7 | 2.27 |
| sparselizar | mumps | 189,408 | -5.378 | 68.3 | 2.1 | 67.4 | 3.05 |

5.14 $c = 0.35$

Table 28: $c = 0.35$ sorted by wall time

| Program | Solver | DOFs | σ_y | Wall [s] | Kernel [s] | User [s] | Memory [Gb] |
|-------------|----------|---------|------------|----------|------------|----------|-------------|
| feenox | gamg | 265,077 | -5.377 | 31.4 | 0.9 | 30.3 | 0.92 |
| calculix | cholesky | 254,881 | -5.375 | 33.7 | 0.4 | 33.2 | 0.30 |
| feenox | mumps | 265,077 | -5.377 | 35.0 | 2.1 | 32.7 | 3.34 |
| reflex | gamg | 265,077 | -5.377 | 39.4 | 1.0 | 38.2 | 1.06 |
| calculix | diagonal | 254,881 | -5.377 | 46.4 | 0.3 | 46.1 | 0.30 |
| reflex | mumps | 265,077 | -5.377 | 46.5 | 2.1 | 44.2 | 3.47 |
| reflex | hypre | 265,077 | -5.377 | 48.7 | 1.2 | 47.4 | 1.32 |
| calculix | spooles | 254,881 | -5.377 | 123.7 | 1.4 | 122.2 | 2.23 |
| sparselizar | mumps | 265,077 | -5.378 | 136.1 | 5.6 | 132.2 | 4.77 |

Table 29: $c = 0.35$ sorted by memory

| Program | Solver | DOFs | σ_y | Wall [s] | Kernel [s] | User [s] | Memory [Gb] |
|-------------|----------|---------|------------|----------|------------|----------|-------------|
| calculix | cholesky | 254,881 | -5.375 | 33.7 | 0.4 | 33.2 | 0.30 |
| calculix | diagonal | 254,881 | -5.377 | 46.4 | 0.3 | 46.1 | 0.30 |
| feenox | gamg | 265,077 | -5.377 | 31.4 | 0.9 | 30.3 | 0.92 |
| reflex | gamg | 265,077 | -5.377 | 39.4 | 1.0 | 38.2 | 1.06 |
| reflex | hypre | 265,077 | -5.377 | 48.7 | 1.2 | 47.4 | 1.32 |
| calculix | spooles | 254,881 | -5.377 | 123.7 | 1.4 | 122.2 | 2.23 |
| feenox | mumps | 265,077 | -5.377 | 35.0 | 2.1 | 32.7 | 3.34 |
| reflex | mumps | 265,077 | -5.377 | 46.5 | 2.1 | 44.2 | 3.47 |
| sparselizar | mumps | 265,077 | -5.378 | 136.1 | 5.6 | 132.2 | 4.77 |

Parametric NAFEMS LE10 benchmark with tet elements

5.15 $c = 0.3$

Table 30: $c = 0.3$ sorted by wall time

| Program | Solver | DOFs | σ_y | Wall [s] | Kernel [s] | User [s] | Memory [Gb] |
|-------------|----------|---------|------------|----------|------------|----------|-------------|
| feenox | gamg | 406,746 | -5.371 | 52.0 | 1.7 | 50.1 | 1.51 |
| calculix | cholesky | 393,259 | -5.368 | 60.8 | 0.6 | 60.2 | 0.46 |
| reflex | gamg | 406,746 | -5.371 | 65.1 | 1.8 | 63.1 | 1.61 |
| feenox | mumps | 406,746 | -5.371 | 72.6 | 3.9 | 68.5 | 5.83 |
| reflex | hypre | 406,746 | -5.371 | 76.6 | 1.9 | 74.5 | 2.01 |
| calculix | diagonal | 393,259 | -5.371 | 87.2 | 0.6 | 86.7 | 0.46 |
| reflex | mumps | 406,746 | -5.371 | 88.5 | 3.7 | 84.6 | 5.92 |
| calculix | spooles | 393,259 | -5.371 | 289.6 | 2.4 | 287.1 | 3.98 |
| sparselizar | mumps | 406,746 | -5.364 | 325.4 | 9.6 | 318.3 | 8.68 |

Table 31: $c = 0.3$ sorted by memory

| Program | Solver | DOFs | σ_y | Wall [s] | Kernel [s] | User [s] | Memory [Gb] |
|-------------|----------|---------|------------|----------|------------|----------|-------------|
| calculix | cholesky | 393,259 | -5.368 | 60.8 | 0.6 | 60.2 | 0.46 |
| calculix | diagonal | 393,259 | -5.371 | 87.2 | 0.6 | 86.7 | 0.46 |
| feenox | gamg | 406,746 | -5.371 | 52.0 | 1.7 | 50.1 | 1.51 |
| reflex | gamg | 406,746 | -5.371 | 65.1 | 1.8 | 63.1 | 1.61 |
| reflex | hypre | 406,746 | -5.371 | 76.6 | 1.9 | 74.5 | 2.01 |
| calculix | spooles | 393,259 | -5.371 | 289.6 | 2.4 | 287.1 | 3.98 |
| feenox | mumps | 406,746 | -5.371 | 72.6 | 3.9 | 68.5 | 5.83 |
| reflex | mumps | 406,746 | -5.371 | 88.5 | 3.7 | 84.6 | 5.92 |
| sparselizar | mumps | 406,746 | -5.364 | 325.4 | 9.6 | 318.3 | 8.68 |

5.16 $c = 0.25$

Table 32: $c = 0.25$ sorted by wall time

| Program | Solver | DOFs | σ_y | Wall [s] | Kernel [s] | User [s] | Memory [Gb] |
|-------------|----------|---------|------------|----------|------------|----------|-------------|
| sparselizar | mumps | 678,393 | -nan | 49.5 | 9.6 | 44.2 | 3.98 |
| feenox | gamg | 678,393 | -5.374 | 96.3 | 2.9 | 93.2 | 2.85 |
| reflex | gamg | 678,393 | -5.374 | 119.8 | 3.2 | 116.3 | 2.92 |
| calculix | cholesky | 659,302 | -5.374 | 125.4 | 1.2 | 124.2 | 0.78 |
| reflex | hypre | 678,393 | -5.374 | 145.9 | 3.5 | 142.2 | 3.35 |
| feenox | mumps | 678,393 | -5.374 | 161.5 | 7.3 | 153.9 | 11.28 |
| calculix | diagonal | 659,302 | -5.374 | 185.2 | 1.0 | 184.2 | 0.78 |
| reflex | mumps | 678,393 | -5.374 | 201.0 | 7.6 | 193.0 | 11.59 |

Parametric NAFEMS LE10 benchmark with tet elements

| Program | Solver | DOFs | σ_y | Wall [s] | Kernel [s] | User [s] | Memory [Gb] |
|----------|---------|---------|------------|----------|------------|----------|-------------|
| calculix | spooles | 659,302 | -5.374 | 814.9 | 4.6 | 810.2 | 7.97 |

Table 33: $c = 0.25$ sorted by memory

| Program | Solver | DOFs | σ_y | Wall [s] | Kernel [s] | User [s] | Memory [Gb] |
|-------------|----------|---------|------------|----------|------------|----------|-------------|
| calculix | cholesky | 659,302 | -5.374 | 125.4 | 1.2 | 124.2 | 0.78 |
| calculix | diagonal | 659,302 | -5.374 | 185.2 | 1.0 | 184.2 | 0.78 |
| feenox | gamg | 678,393 | -5.374 | 96.3 | 2.9 | 93.2 | 2.85 |
| reflex | gamg | 678,393 | -5.374 | 119.8 | 3.2 | 116.3 | 2.92 |
| reflex | hypre | 678,393 | -5.374 | 145.9 | 3.5 | 142.2 | 3.35 |
| sparselizar | mumps | 678,393 | -nan | 49.5 | 9.6 | 44.2 | 3.98 |
| calculix | spooles | 659,302 | -5.374 | 814.9 | 4.6 | 810.2 | 7.97 |
| feenox | mumps | 678,393 | -5.374 | 161.5 | 7.3 | 153.9 | 11.28 |
| reflex | mumps | 678,393 | -5.374 | 201.0 | 7.6 | 193.0 | 11.59 |